

Accurate Radiation Pattern Measurements in a Time-Reversal Electromagnetic Chamber

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ABSTRACT

In a recent paper [1], we have introduced the concept of the time-reversal electromagnetic chamber (TREC), a new facility for creating coherent wave-fronts within a reverberation chamber. This facility, based on the use of time-reversal techniques in a reverberating environment, is here shown to be also a useful tool for the characterization of the field radiated by an antenna under test (AUT). The TREC is proven to be capable of providing real-time measurements, with an accuracy comparable to that of spherical near-field facilities, while using a very limited number of static probe antennas. This performance is made possible by taking advantage of the reflections over the chamber's walls, in order to gain access to the field radiated along all the directions, with no need to mechanically displace the probes, or to have a full range of electronically switched ones. A 2D numerical validation supports this approach, proving that the proposed procedure allows the retrieval of the free-space radiation pattern of the AUT, with an accuracy below 1 dB over its main lobes.

Keywords: Radiation Pattern, Time Reversal, Reverberation Chamber, Real Time, Time Domain.

1. Introduction

Historically, facilities for the characterization of antenna radiation can roughly be divided into two classes, one based on the mechanical displacement of one single probe [2, 3], the second using electronic switching of an array of probes in order to speed up the measurement [4]. This classification holds for both near and far-field facilities. According to the industrial context of utilisation, the two systems are interesting solutions: indeed, the electronic switching configuration is by far more complex and expensive, and its use is justified only in case of need for fast measurements. Being both based on the use of anechoic chambers, in order to have the antenna under test (AUT) radiation measured along a given direction,

the probe must be aligned along it. Hence, the need for a fine mesh of sample positions for characterizing the AUT. In this paper, we propose a change of paradigm, by candidating a reverberation chamber (RC) as a counter intuitively simpler environment for antenna testing. Although apparently useless for such a purpose, due to the high-echo content of any signal measured in it, we provide a procedure that allows deembedding the actual free-space radiation pattern (RP) of the AUT. Among its several interesting features, this solution allows carrying out a complete characterization of the AUT radiation with no need to have the probes aligned to the directions of interest. This is basically due to having exploited the reflections over the cavity walls for accessing several directions at the same time. For the same reason, the number of probes required can be reduced, while maintaining a level of accuracy below 1 dB around the RP maxima. These advantages come with a price tag, since the cavity needs to be characterized experimentally before being able to retrieve the antenna RP in free-space, thus making this solution not suitable for one-time antenna characterizations.

2. The time-reversal electromagnetic chamber

A time-reversal electromagnetic chamber (TREC) is a facility capable of generating coherent wave-fronts inside an RC [1]. It basically exploits the properties of time reversal techniques, by ideally reversing the time-evolution of a field distribution originally generated by a given source of radiation. A TREC is constituted by an RC, where an array of M probe antennas are installed, generally near its walls, usually referred to as the time-reversal mirror (TRM) antennas. These are the only active antennas, in the setup. Conversely, a second array of probes is distributed at the centre of the TREC, over a, usually, closed surface. This second group is constituted by ideal elementary dipoles, employed as E field probes. Their role is limited to sampling the E field at their location, for a given polarization, hence their being considered as virtual probes, since they will be assumed to be transparent, giving rise to no scattering phenomena.

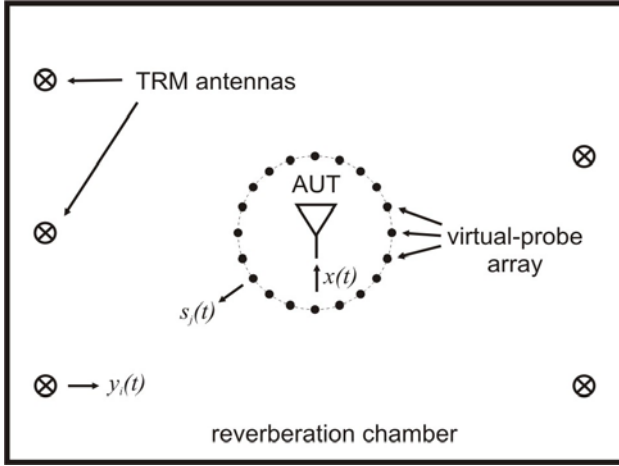


Figure 1 – Synoptic of the TREC system. The signals refer to the characterization phase.

Real-life devices approximating this scenario exist, such as Enprobe’s all-optical probe EFS-105.

The virtual-probe array has a fundamental role, since, it allows characterizing the transmission of energy between the TRM and the region of space where a device under test (DUT) is considered for EMC purposes. The procedure introduced in [1] allows to define time-domain signals $y_i(t)$ to be applied to each of the TRM antennas in order to have them generating a coherent pulsed wave-front propagating and focusing towards the DUT, along any direction, without any need to mechanically move the TRM antennas around the DUT. This remarkable result is made possible by exploiting the reflections over the walls of the cavity, thus allowing to access the DUT along an ideally continuous range of directions.

In this paper, we prove that this technique can also be applied to the measurement of antenna RPs, and that it comes with a number of interesting features. Before going further, we need to recall some major results from time-reversal theory. It has been shown in [5] that given a source of radiation in a resonant cavity, excited by a pulsed signal, and a collection of transducers acting as a TRM, the signals received by the transducers can be used for transmitting back on the former source a pulse that is very close to the original one. The ability of creating coherent transmission in a cavity was extended from a point-to-point configuration to coherent wave-fronts in [1], by introducing the idea of a virtual-array “wrapped” around a test region. Now, by considering the source of radiation to be an AUT, these precedents imply that the signals received by the TRM antennas could be used for recreating the field radiated by the AUT in the first place. The missing link for transforming this idea into an RP measurement facility is a theoretical tool for relating the signals received on the TRM antennas to the signals that

would be measured when the AUT is radiating in free-space. This tool is derived in the next Section.

Although this technique can be applied to a full 3D configuration, we will limit for the scope of this paper to a 2D case. The reason for this choice is based on the need to firstly introduce these ideas and testing their feasibility, and because the 2D case can be used for imposing a scalar electric field. We stress the fact that preliminary experimental and numerical results show that it is possible to address the polarization of the field even with linearly polarized TRM antennas, with no need to rotate them as in anechoic chambers, thanks to the depolarization properties of RCs. These results will be presented in a future paper.

3. Reconstruction of the radiation pattern

Let us consider a test signal $x(t)$ applied to the AUT. Its choice depends on its spectral content, as it is intended for soliciting the response of the AUT over a given frequency range $F = [f_1, f_2]$. Nevertheless, an infinity of signals sharing the same spectral content can be considered. The best choice for the purpose we have set is to have it pulse-like and with the smallest time-domain support. This requirement is dictated by the fact that the propagation inside an RC can be assimilated to free-space as long as the pulsed EM field excited by the antenna does not interact with the cavity walls. Free-space propagation occurs over a short time-window lasting $T = d/(2 c_0)$, where d is the shortest lateral dimension of the RC and c_0 is the speed of light in air. In order to retrieve the free-space radiation, it is necessary that the pulsed field radiated by the AUT have a support smaller than T . During this time-window, the virtual probes would receive the signals $s_i(t)$ that are the basis for any free-space antenna measurement procedure. Therefore, the positions of the virtual probes need to be designed as for a classic near-field facility.

As the field radiated by the AUT reaches the TRM antennas, signals $y_i(t)$ will be received on them. If we were to apply the classical time-reversal procedure [6], exciting the TRM antennas with the signals $y_i(-t)$ would lead to signals $\hat{s}_j(-t)$ measured over the virtual probes. These signals are a close replica of the signals $s_j(-t)$. Let us now assume to know the pulse responses $h_{ij}(t)$ characterizing the transmission channel between the i -th TRM antenna and the j -th probe of the virtual-probe array. In this case, we can state that:

$$\hat{s}_j(t) = \sum_{i=1}^M y_i(-t) * h_{ij}(t) \quad , \quad (1)$$

so that as $\hat{s}_j(-t) \approx s_j(t)$, equation (1) provides a way of directly linking the signals measured on the TRM antennas to the wished ones around the AUT, at the

virtual probes locations. Applying the Fourier transform to (1), yields:

$$\hat{S}_j(f) = \sum_{i=1}^M Y_i^*(f) H_{ij}(f) \quad . \quad (2)$$

These results highlight the fundamental importance of the transfer functions $H_{ij}(f)$, since acceding to them would allow providing an estimate of the field radiated near the AUT, while carrying out the actual measurement far from it and with no need for linking the TRM antennas positions and those of the virtual probes. The measurement of $h_{ij}(t)$ is the topic of Section 5. The analysis leading to (2) can be pushed further, linking the actual signals $S_j(f)$ to the estimated ones $\hat{S}_j(f)$.

To this end, we invoke Huygens principle, recalling that the signals $Y_i(f)$ can be expressed as the superposition of the contributions coming from each elementary source $S_j(f)$:

$$Y_i(f) = \sum_{j=1}^N s_j(f) H_{ij}(f) \quad . \quad (3)$$

Organizing the signals into column vectors, and the transfer functions into the channel matrix \mathbf{H} , we get:

$$\hat{\mathbf{S}}^* = \mathbf{H}^H \mathbf{H} \mathbf{S} = \mathbf{K} \mathbf{S} \quad , \quad (4)$$

where the apex H stands for the Hermitian operator.

This result states that in order to have a good estimate of the field radiated by the AUT, matrix \mathbf{K} needs to have a dominant main diagonal, with the value of its elements as close as possible. A complete analysis of how the properties of the \mathbf{K} matrix are linked to the spatial correlation in an RC is unfortunately unfeasible in the present context, since it would take much space. Nevertheless, it can be summed up considering two issues: 1) the correlation between the TRM antennas and 2) that between the virtual probes. The TRM antennas need to be ideally uncorrelated, in order to have each one providing new degrees of freedom, and thus an improvement in the field retrieval algorithm (see Section 7). To this end, it is necessary to ensure a minimum distance of half the wavelength at the minimum frequency f_l [7]. Conversely, this requirement is not necessary for the ideal probes, since as frequency decreases and the ideal probes start to be correlated, the maximum distance needed for computing the far-field of the AUT increases. This means that adjacent ideal probes will indeed be correlated, but it is no more necessary to consider the output of each probe, since the actual Shannon sampling distance requires a decimation of the virtual-probe array. It would rather be better to consider a

sort of a sliding spatial average. This operation is implicitly accomplished by the harmonic filtering exposed in the next Section.

Signals measured in an RC are affected by long transients. Nevertheless, it was shown that the time-reversal technique attains its maximum performance after a time approximately equal to the modal density of the cavity [5]. For the system considered in Section 6, this happens after about 600 ns. This also set the duration of any measurement in this TREC, which is thus very fast, not requiring any additional mechanical movement.

A last important point is that since time-reversal approximates the entire propagation of the field radiated by the antenna, and this being strongly affected by the presence of reflective walls, signals $\hat{s}_j(t)$ will also contain a broad range of echoes, and not just the pulse radiated by the AUT during the free-space time window. It is thus necessary to apply a gating function to the $\hat{s}_j(t)$, hence the reason for the requirement of having the pulse radiated by the antenna to be sufficiently isolated from the first echoes. Due to this constraint, the use of the proposed procedure can be critical as soon as the AUT becomes resonant and poorly efficient, since in this case it would radiate long undamped harmonics that could exceed the free-space time window, so that it would be impossible to separate the direct radiation from the first echoes coming from the walls .

4. Angular harmonic filtering

As shown in Section 6, the reconstructed field is characterized by fast angular variations that are not physical for far-field propagation. Since time reversal operates as a propagation operator, no reactive component of the originally radiated field could be generated, so that these variations must be related to the imperfect reconstruction (see Section 7). An effective way of filtering them out of the estimated RP is to apply the procedure described in [8], i.e., by limiting the Fourier series expansion of the RP to its first N terms, with N given by

$$N = \lceil kR \rceil \quad , \quad (5)$$

where R is the radius of the smallest circle containing the AUT, and k is the wave-number. These N terms correspond to the cylindrical harmonics that would indeed propagate in free-space. Although for a different reason, this truncation is to be applied also to the RP derived from the $s_j(t)$ measured over the virtual-probe array during the free-space time window: in this case it is needed for filtering the reactive components of the field excited by the AUT, since at low frequencies the probes will not meet the far-field distance condition.

5. Medium characterization

We have shown in Section 3 the central role played by the channel matrix \mathbf{H} . The application of the proposed method is conditioned by the availability of an accurate estimate of this matrix. Since the virtual probes are not intended for emission, but just for sampling the E field, one way of measuring the $H_{ij}(f)$ functions is to feed each TRM antenna with a test signal $x(t)$, while measuring the signals $p_i(t)$ received at the virtual probes locations. The transfer functions $H_{ij}(f)$ can thus be computed by means of a direct deconvolution

$$H_{ij}(f) = \frac{P_j(f)}{X(f)}, \quad (6)$$

having applied $x(t)$ to the i -th TRM antenna. Equation (6) is well-defined as long as $X(f)$ has no zero-crossings: this is the case, e.g., for Gaussian pulses. The main difficulty in obtaining the channel matrix is clearly the need for an array of ideal probes. This scenario can be very well approximated by using phase-preserving all-optical E-field probes, such as Enprobe's EFS-105. Rather than deploying an actual array of such probes, the negligible scattering they provide means that the probe can be moved around the AUT, while collecting the $H_{ij}(f)$. Clearly, this is the same scenario underlying any near-field radiation-pattern measurement, so that one could ask whether the proposed method is sensible. The key for understanding its interest is that as long as the channel matrix \mathbf{H} stays unchanged, it needs not be characterized again. This rules out using the TREC-based method for one-time blind characterizations; conversely, it is an interesting alternative to existing facilities in at least two real-life situations: 1) mass-produced radiating equipments, where the field they radiate may change, due to manufacturing tolerances/faults, while maintaining exactly the same mechanical structure and 2) large phased-arrays where the number of radiation configurations can be quite high, leading to a long characterization time. These two configurations share a common feature, i.e., the presence of a static mechanical configuration, while the field radiated by the AUT can change. Indeed, the use of the TREC requires dissociating free-space radiation and propagation inside it.

A final consideration about the channel matrix is necessary: recalling the results from RC theory, the sensitivity of any transfer function to mechanical displacements is related to their electrical distance. Indeed, the spatial correlation stays high as long as the displacements involve distances shorter than $\lambda/8$ [7].

6. Numerical results

The proposed method was studied by means of numerical simulations, carried out in the time domain thanks to

CST's Microwave Studio. The cavity was a quasi-2D one, with transversal dimensions of 8×6.4 m², and a thickness of 15 cm, hence enforcing the existence only of purely transversal resonant modes. The fact of having the two main walls made out of a perfect electric conductor, and at a distance that is electrically small over the entire frequency range, implies that the E field is almost scalar and propagating over a planar surface. This configuration has allowed the introduction of the simplified model presented in Section 3.

Twelve TRM antennas were placed along two facing walls, six by side, in a way similar to that of Fig. 1. The distance between adjacent TRM antennas was fixed at about 1 m, which ensures that their responses are well uncorrelated down to 100 MHz. The distance between the TRM antennas and the walls was set at 30 cm; the only requirement is that the walls do not short-circuit too much the antennas. Half-wavelength dipoles were used, resonating at 1 GHz. A virtual-probe array made up of 64 ideal probes was considered, uniformly distributed over a circumference 2 m wide in diameter, thus respecting Shannon sampling theorem up to 1.5 GHz in free-space for propagative field components.

The AUT was a four-element uniform linear array constituted by the same dipoles as the TRM antennas. The axis of the array was tilted of a 45-degree angle in order to avoid long propagation patterns in the case of broadside radiation. The array was chosen since it allows checking one of the most important features of the TREC-based system, i.e., that as long as the mechanical/propagation configuration of the cavity-AUT system are unmodified, the same channel matrix \mathbf{H} can be applied. To this end, the array was fed with several phase-shifts, in order to tilt the main radiation lobe. The AUT was excited with a base-band Gaussian pulse, covering frequencies up to 1.5 GHz. After applying the characterization procedure detailed in Section 5, the AUT was finally excited, and the TRM signals recorded. Time-domain signals over the virtual-probe array was retrieved by means of the technique proposed in Section 3. An example is shown, for a broadside radiation, in Fig. 2. Indeed, the pulsed field radiated by the AUT is well identified, even though the number of TRM antennas is a sixth of the number of probes that would be necessary in a near-field free-space setup. Fig. 2 shows that the reconstructed field is affected by spurious propagation traces, due to the limited number of resonant modes involved. The obtained results prove that the free-space assumption holds, since the first echoes are seen over the probe array only after 23 ns (not shown), so that a gating over the first 11 ns allows removing them. Although the right-end of the gating interval can be freely placed between 7 and 23 ns, the choice of the left-end is much more critical. This is due to the fact that the signals reconstructed through time-reversal are related to a wave-

front very similar to the one originally emitted by the AUT, but moving back towards it. Hence, the first 3 ns deal with the field that would be scattered back by the AUT and measured by the virtual-probe array. This contribution is thus unwanted and must be accurately removed.

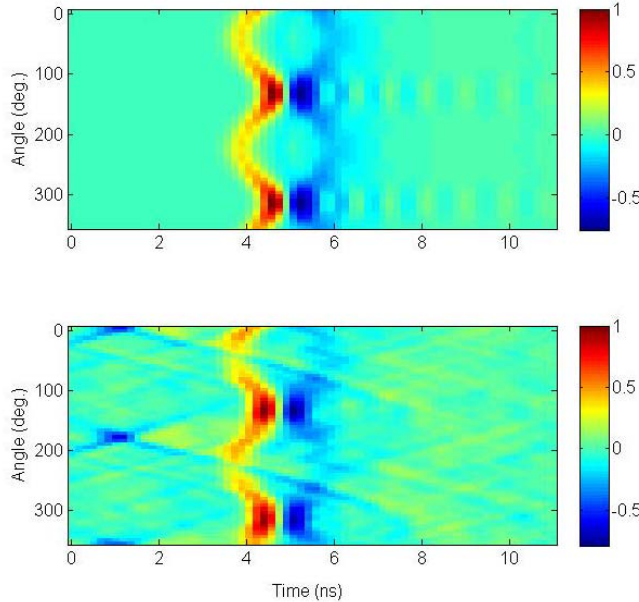


Figure 2 – Time-domain reconstruction of the E field radiated by the AUT during the free-space time window. The two sets of signals have been normalized to their peak value.

By Fourier-transforming the time-domain results, the field radiated by the AUT under a CW excitation can be retrieved. Fig. 3 presents a few RPs obtained after applying the angular harmonic filtering described in Section 4. Two feeding configurations were considered, for a tilt angle of zero degrees (with respect to the broadside direction) and 45 degrees. As a matter of fact, the free-space RPs are very well characterized, presenting a maximum error below 1 dB over the first 10 dB range. As expected in any retrieval procedure, the most critical parts are the nulls. These results prove that indeed, if the AUT is to be tested for several radiation configurations, while maintaining a static mechanical setup, the proposed procedure is indeed interesting, allowing a full characterization with less signals to be measured, over a period of just a fraction of a microsecond.

7. On the quality of the reconstruction

The concept of quality can be formalized by recalling that the reconstructed field can be regarded as given by the superposition of a coherent part, i.e., the original signal to

be estimated and an incoherent one, i.e., the residual noise in the reconstruction. The quality is thus given by the square of the ratio of the amplitude of the coherent part and the incoherent one [5]. Interestingly, it can be assimilated to a signal to noise ratio.

The accuracy of the reconstruction can be shown to depend on two issues, the number of resonant modes excited in the cavity and the number of TRM antennas. The former is the most important one, since it does not lend itself to modifications introduced by the designer. Indeed, the resonant behaviour of the cavity is a function of the frequency, and it is strongly related to the physical dimensions of the cavity as well as the conductivity of the materials involved; in other words, the quality factor of the cavity. As long as the cavity is strongly resonant, it can be shown that the quality of the reconstruction is directly proportional to the number of modes excited over the bandwidth spanned by the test pulse $x(t)$ [5]. Since this goes as the square of the frequency, the reconstruction is expected to get better at the higher frequency end.

In order to understand how the number of TRM antennas impact the quality of the reconstruction, it is necessary to assume that their electrical distance is sufficiently high as to ensure a very low correlation between the transfer functions relating a given virtual probe to a pair of TRM antennas. Under these conditions, the contribution of each TRM antenna to the reconstructed field will be uncorrelated from the others, so that the residual incoherent noise will sum up in energy and not in amplitude, whereas the opposite will be true for the coherent part. This means that the quality of the reconstruction grows like M . Hence, the number of TRM antennas plays a minor role with respect to the number of resonant modes excited. Nevertheless, as the frequency decreases, the number of modes reduces, so that increasing the number of TRM antennas is a viable solution for improving the performance of the TREC-based system.

8. Conclusions and perspectives

In this paper we have proven that, against received wisdom, RCs can be an interesting alternative to anechoic chambers as facilities for accurately characterizing the RP of an AUT. A modified RC configuration was advocated, the TREC, which among other advantages allows reducing the number of probe antennas needed for the measurement, as well as avoiding all mechanical movement, leading to full characterizations in less than a microsecond. These features are made available by the use of a theoretical procedure that allows retrieving the free-space field radiated by the AUT, thanks to the properties of time-reversal techniques. A medium characterization procedure being necessary, this technique is not suitable for one-time characterizations,

but it proves to be powerful as soon as static/repetitive configurations are involved, so that the same channel matrix can be applied, leading to a strong reduction of the characterization time. Despite the present analysis focuses on a scalar 2D chamber, it can be proven that this technique can be extended to a full 3D vector configuration, without any need to consider more complex TRM antennas, while avoiding any mechanical movement. These results are of course just preliminary to a full-scale validation involving a 3D TREC.

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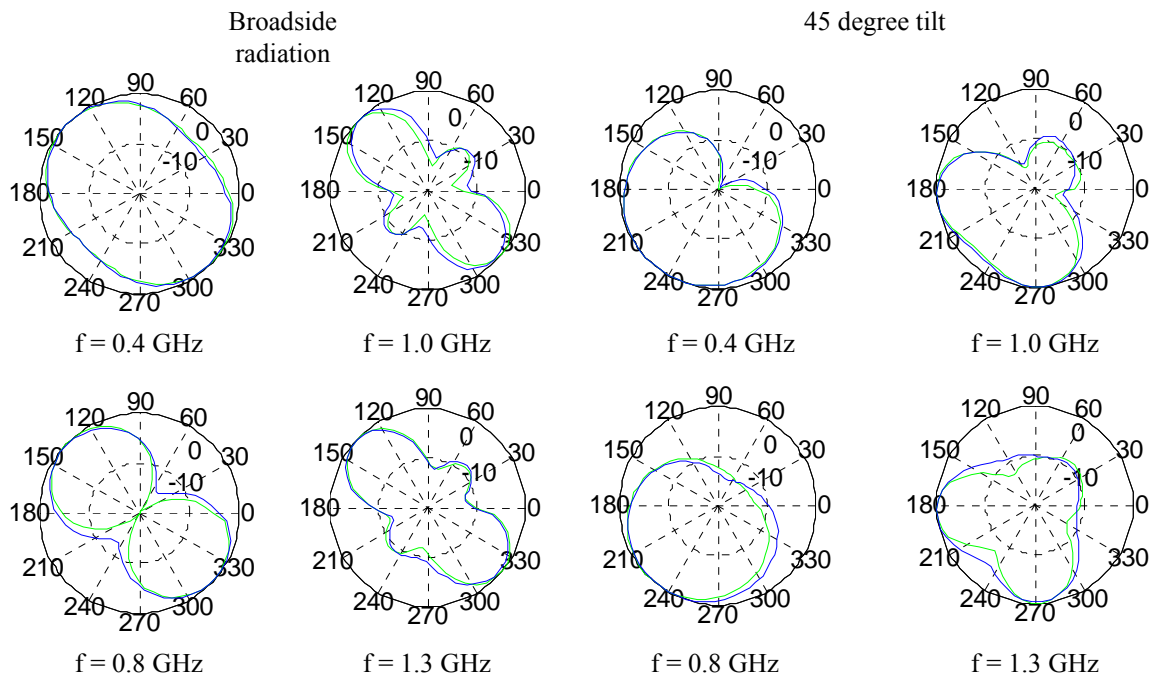


Figure 3 – Some results from the numerical validation, comparing the RPs derived from the E field as measured over the virtual probes during the free-space time window (green lines) and those retrieved from signals measured on the TRM antennas (blue lines). The RPs are represented on a 20 dB dynamic range. The tilt of 45 degrees is due to the fact that the axis of the array was tilted of this same angle in order to avoid long propagation times in the case of a broadside radiation.